# CS 61BL Heaps and Graphs <br> Summer 2021 <br> Quiz 10: Friday July 30, 2021 

1 Graph Representations


In the parts below, enter the adjacency list corresponding to each node.
For every part, your answer should be sorted by least to greatest with a single space between each item. For example, a node A that has edges to nodes D, C, and B would be input as: B C D
a) What is the adjacency list for node 0 ?
b) What is the adjacency list for node 1 ?
c) What is the adjacency list for node 2 ?
d) What is the adjacency list for node 4 ?

## 2 Heaps

We have the following heap, representing a Min PQ: [-, 1, 4, 6, 7, 10, 12, 15,
16]. Here, - represents null.
a) What is the left child of element 4?
( ) $6 \$ 7() 10() 12$
b) What is the right child of element 6 ?
( ) 7 ( ) 10 () $12{ }^{15}$
c) Suppose we insert 0 . What is the resulting state of the heap?
() $[-, 1,0,6,4,10,12,15,16,7]$
( $[-, 0,1,6,4,10,12,15,16,7]$
() $[-, 0,1,4,6,7,10,12,15,16]$
( ) None of the above
d) Consider the initial state of the heap again. $[-, 1,4,6,7,10,12,15,16]$

Suppose we call removeMin(). What is the resulting state of the heap?
() $[-, 4,6,7,16,10,12,15]$
() $[-, 4,7,6,15,10,12,16]$
() $[-, 6,4,12,7,10,16,15]$

X [-, 4, 7, 6, 16, 10, 12, 15]
( ) None of the above

$\begin{array}{llll}\rightarrow & 16 \\ 4 & 4 & 6 & \\ 7 & 10 & 12 & 15\end{array}$

## 3 Graphs

Suppose we have the graph below.


For all parts below, assume we break ties alphabetically.
a) What is the order that vertices are visited if we run DFS preorder starting on vertex A? Enter your answer as a space separated list, e.g. A B C D E F G.
b) What is the order that vertices are visited if we run DFS postorder starting on vertex A? Enter your answer as a space separated list, e.g. A B C D E F G.
c) What is the order that vertices are visited if we run BFS starting on vertex A ? Enter your answer as a space separated list, e.g. A B C D E F G.

2 Heap Mystery
We are given the following array representing a min-heap where each letter represents a unique number. Assume the root of the min-heap is at index zero, i.e. A is the root. Note that there is no significance of the alphabetical ordering, i.e. just because B precedes C in the alphabet, we do not know if B is less than or greater than C.Array: $[\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E}, \mathrm{F}, \mathrm{G}]$
Four unknown operations are then executed on the min-heap. An operation is either a removeMin or an insert. The resulting state of the min-heap is shown below.

Array: [A, E, B, D, X, F, G]
(a) Determine the operations executed and their appropriate order. The first operation has already been filled in for you!

1. removeMin()
2. 


3. renove (c)
4. insert $(A)$
(b) Fill in the following comparisons with either $>,<$, or ? if unknown. Note that this question does not assume a specific ordering of operations from the previous part, i.e. we don't know which of the two possible

1. x 2 D
2. $\mathrm{x} \geq \mathrm{C}$
3. $\mathrm{B} \geq \mathrm{C}$
4. $\mathrm{C}<\mathrm{x}$


Major Differences:


